Laboratory exercises

Laboratory rules

Laboratory work organization

Lab safety rules – students' signature !!

Assessment conditions (deadline by 15th February 2026)

compulsory practical lab measurements (fully passed)

successful delivery of **all** measurement reports (A - E)

Important notes (see the work organization):

14 days for the report delivery

maximum number of F classifications = **5**

maximum number of compensatory measurement dates = 5

1st measurement – Task Nr. 0 (2nd term week)

Measurement and processing of time and dimensions data

Homework – read the instructions!

Laboratory groups (by 4th term week)

Laboratory measurements timetable – task Nr. 0 + 4 tasks

measurement every 2 weeks

the other weeks – presentations

theory of the next tasks

knowledge testing – oral examination

notes are allowed

Measurement report

A well-organized measurement report consist of:

- heading with the task name (website)
- specification of the task
- theoretical principle of the task
- definition of all important quantities with units
- short description of the measurement procedure
- wiring diagrams (if needed)
- a list of uncertainty calculation formulas
- clear general solution of the physical formulas
- precise values substitution and calculation of results with physical units (uncertainty calculation included)
- supplement sheets with the data regression (if needed)
- a list of the data signed by the teacher

Preparation par

ost-processin

Theory of uncertainty

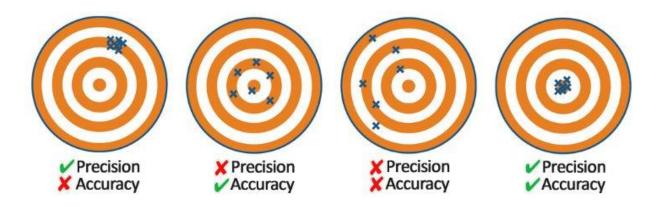
measurement - estimation of level of confidence

exact (true) value — hard to get in a real measurement

definition of range that surely includes true value

measurement = (best estimate ± uncertainty) {physical unit}

accuracy = ability to get the result near the true value
precision = ability to get a narrow range of obtained data
true value can be outside this range (inaccurate) !!



Error vs. Uncertainty

measurement errors = difference between the measured value and the 'true value'

measurement uncertainties = quantification of the doubt about the measurement result

Expression of Errors

Absolute Error K_x of a quantity X

same unit as the physical quantity

Relative Error of a quantity X

ratio of absolute error to the value of quantity

$$\kappa_{rx} = \frac{\kappa_{x}}{x}$$
 relative value (no unit)

Types of Errors

Random Errors = statistic fluctuations of results

due to precision limits of the tool (instrument)

could be reduced by averaging of large number of data

Systematic Errors = reproducible inaccuracies

hard to detect, impossible to analyse by statistics

sometimes predictable by instrument calibration

Estimating of the Errors - single measurements

Dimensions: standard error $m_{x} (= \kappa_{x})$

Tape measure: $m_x = 1 \text{ mm}$

Calliper: $m_x = 0.1 \text{ mm}$

Micrometre: $m_x = 0.01 \text{ mm}$





Time: stop-watch standard error $m_x = 0.01 \text{ s}$ human reaction time $m_x = 0.5 \text{ s}$



Electrical quantities – analogue instruments

accuracy class T_p

≈ maximum relative error within selected range x_{max}

$$m_{x} = \frac{1}{100} T_{p} x_{\text{max}}$$



Electrical quantities – digital instruments



example from user's manual: $m_x = 0.01\%$ rdg. + 2 digits

base error = percentage of the obtained value (reading)
digits of instrument resolution = dependent on the range
last digital place (considering the decimal place)
e.g. *U* = 12.778 V → one digit ≈ 0.001 V

Estimating of the Errors - repeated measurements

mean (average) value $\overline{x} = \frac{\sum_{i=1}^{n} x_i}{x_i}$

$$\overline{x} = \frac{\sum_{i=1}^{n} x_i}{n}$$

standard deviation of the mean value (data spread)

$$S_{\overline{x}} = \sqrt{\frac{\sum_{i=1}^{n} (\overline{x} - x_i)^2}{n(n-1)}}$$

Uncertainties

Type A = uncertainty estimated by statistics

Type B = other sources (instrument errors, etc.)

Expression of Uncertainty

Absolute uncertainty u_x of a quantity X

same unit as the physical quantity

Relative Uncertainty u_{rx} of a quantity X

ratio of absolute error to the value of quantity

$$u_{rx} = \frac{u_x}{X}$$
 "r" for "relative" relative value (no unit)

Uncertainty for a Type A evaluation

$$u_{xA} = s_{\overline{x}} = \underbrace{\sum_{n=1}^{n} (x_i - \overline{x})^2}_{n(n-1)}$$

Uncertainty for a Type B evaluation

$$u_{zB} = \frac{\Delta z_{\text{max}}}{\chi}$$

 $u_{zB} = \frac{\Delta z_{\text{max}}}{\gamma}$ Δz_{max} is the maximum of all detectable systematic errors (= m_x) systematic errors (= m_x)

$$\chi = \sqrt{3}$$

 $\gamma = \sqrt{3}$ for the uniform distribution

Combining standard uncertainties A and B Type

law of summation in quadrature $u_x = \sqrt{u_{xA}^2 + u_{yR}^2}$

$$u_x = \sqrt{u_{xA}^2 + u_{xB}^2}$$

Combining standard uncertainties – general approach

for quantity
$$Y = f(X_1, X_1, ..., X_n)$$

$$u_Y = \sqrt{\left(\frac{\partial Y}{\partial X_1}\right)^2 u_{X_1}^2 + \left(\frac{\partial Y}{\partial X_2}\right)^2 u_{X_2}^2 + \dots + \left(\frac{\partial Y}{\partial X_n}\right)^2 u_{X_n}^2}$$

Calculation of sum for Type A and Type B estimation

a set of sub-uncertainties $u_{X_1A}, u_{X_2A} \dots u_{X_nA}, u_{X_1B}, u_{X_2B} \dots u_{X_nB}$

$$u_{YA} = \sqrt{\left(\frac{\partial Y}{\partial X_1}\right)^2 u_{X_1A}^2 + \left(\frac{\partial Y}{\partial X_2}\right)^2 u_{X_2A}^2 + \dots + \left(\frac{\partial Y}{\partial X_n}\right)^2 u_{X_nA}^2}$$

$$u_{YB} = \sqrt{\left(\frac{\partial Y}{\partial X_1}\right)^2 u_{X_1B}^2 + \left(\frac{\partial Y}{\partial X_2}\right)^2 u_{X_2B}^2 + \dots + \left(\frac{\partial Y}{\partial X_n}\right)^2 u_{X_nB}^2}$$

$$u_Y = \sqrt{u_{YA}^2 + u_{YB}^2}$$

Simplification for two quantities in basic operations

values **a** and **b** are real constants **m** and **n** are natural indices

Operation	Formula	Uncertainty calculation
Addition or subtraction	$Y = X_1 \pm X_2$	$u_Y = \sqrt{u_{X_1}^2 + u_{X_2}^2}$
	$Y = aX_1 \pm bX_2$	$u_Y = \sqrt{a^2 u_{X_1}^2 + b^2 u_{X_2}^2}$
Multiplication or division	$Y = X_1 X_2$	$u_{rY} = \sqrt{u_{rX_1}^2 + u_{rX_2}^2}$
	$Y = aX_1^m X_2^n$	$u_{rY} = \sqrt{m^2 u_{rX_1}^2 + n^2 u_{rX_2}^2}$

Expression of the result

$$Y \pm u_Y$$

uncertainty value - round up in all the cases number of significant figures = 2

result Y - same number of decimal places as the uncertainty

$$\lambda = (632.8 \pm 1.3) \text{ nm}$$
 $T = (1.235 \pm 0.032) \text{ s}$
 $E = (2.05 \pm 0.12).10^{11} \text{ Pa}$